

令目標函數 $z = f(x, y) = 3x + y$, 依照題義得到三個端點 $(2, 2), (2, 4 - c), (\frac{c+4}{3}, \frac{8-c}{3})$

因為 $f(x, y)$ 的最小值是5, 所以最大值若存在必定會在 $(2, 4 - c)$ 或 $(\frac{c+4}{3}, \frac{8-c}{3})$

其中, $f(2, 2) = 8, f(2, 4 - c) = 10 - c, f(\frac{c+4}{3}, \frac{8-c}{3}) = \frac{2c}{3} + \frac{20}{3}$

Case(i)

$\frac{2c}{3} + \frac{20}{3} = 5$ 且 $\frac{2c}{3} + \frac{20}{3} < 10 - c \Rightarrow c = \frac{-5}{2}$ 且 $c < 2, f(2, 4 - c) = 12.5$

Case(ii)

$10 - c = 5$ 且 $10 - c < \frac{2c}{3} + \frac{20}{3} \Rightarrow c = 5$ 且 $c > 2, f(\frac{c+4}{3}, \frac{8-c}{3}) = 10$

By(i), (ii) \Rightarrow 得到最大值12.5